

STUDY OF THE PRIMARY CONVERTER-OBJECT SYSTEM FOR ELECTROCHEMICAL DEVICES

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Abstract. The problem of creating electrochemical devices and the issues that arise in the system of the primary converter-object of control are considered. Low-resistance (salt solutions) and high-resistance (sugar solutions) objects were selected as the subject of study. To solve the problem, we have applied the method of impedance spectrum analysis with EIS Spectrum Analyzer software, which performs modeling on the Levenberg–Marquardt algorithm. Substitution schemes in different frequency and concentration ranges of studied objects were synthesized. This enables appropriate corrective action to minimize the impact of adverse events in the system while monitoring the quality of solutions – non-electrical nature objects – by electrochemical devices.

Key words: Electrochemical devices; Impedance spectra; Non-electrical nature object; Substitution scheme; Computer simulation; Primary converter.

1. Introduction

Since the basic concept of the work is the evaluation of objects as a system and the development of methods for quality indicators assessment aimed at the application of advanced methods. The properties of this system can be studied. Its behavior can be predicted in different conditions, reflecting its corresponding substitution scheme (equivalent scheme). If the impedance is the general method that characterizes the behavior of the whole studied electrochemical system, then impedance modeling becomes necessary for the study of electrochemical kinetics and electrochemical systems in general by constructing model structures. These structures consist of individual elements [1–3].

For different types of electrode systems (for example, different materials – platinum, stainless steel, graphite) while studying the same object, the frequency dependences of the admittance are obtained, that differ in shape. To correctly interpret the admittance spectra, as well as to understand the processes occurring at the boundary of the studied Object – Primary Converter, it is necessary to analyze the admittance spectra and model electrochemical systems.

Modeling can be performed in two ways, one of which is the classical approach, based on the acceptance of hypotheses about the specifics of the object under study and the compilation of a system of differential equations [4, 5]. This approach is logically correct, but the complexity of real models, which often cannot be solved, limits the possibilities of the approach. Often simplifications need to be made. This may contradict the basic conditions of the experiment, so it is necessary to look for new analytical solutions with minor changes in the original hypothesis. Therefore, the derived equation of the dependence of the impedance on the electrochemical parameters may contain more elements than practically determined elements.

Structural modeling should be used to overcome these shortcomings. It is based on a systematic approach

to objective analysis. It is considered a system of electrical elements connected. The structural model becomes completely adequate to the structure of the corresponding equation but contains fewer parameters required to describe the impedance in a certain frequency range [6–8]. Structural impedance models contain quantitative information about the behavior of the object under study in the frequency range, as well as information about the physics of the processes. If the system Primary Converter – Object of control is presented in the form of a passive bipolar, then the interconnected basic elements such as resistors, capacitors, and inductors will be its parameters. It is possible to reproduce the inner structure of the bipolar according to the impedance frequency spectra and construct an equivalent circuit. While monitoring the non-electrical nature objects (in particular the solutions) it happened that the solution-electrode system undergoes processes that cannot be described by a finite number of elements.

Thus, at the electrode-solution interface, an electrode electric layer is formed, the phenomena of charge diffusion (transfer of ion charge to the electrode surface) occur, and electrochemical reactions take place on the electrode surface. Then becomes necessary to pass to a higher level of synthesis of bipolar. It is necessary to apply special electrochemical elements, which physically correspond to the processes modeled by them [9–11].

The electrical properties of the contact surface of the electrode and the test object – solution, are very important for the design of devices for determining electrochemical quality indicators because during modeling it is possible to detect parasitic parameters (electrode parasitic capacitance, additional impedance electrodes, additional impedance due to the formation of fractals, getting into the oxygen solution during contact of the electrochemical cell surface with air, violation of the ideal polarization of the electrodes and, consequently, the emergence of additional impedance

due to electrochemical reaction on the electrodes, etc.). Identification of these features makes it possible to take appropriate corrective action minimizing the impacts in the system Primary Converter – Object during monitoring the quality of non-electrical nature objects by electrochemical devices.

2. Disadvantages

The known substitution schemes for objects do not contain information about the frequency range and features of the application of different nature electrochemical systems.

3. Goal

Investigation of the impedance spectra of low-impedance and high-impedance objects aiming correct selection of the design parameters of electrochemical transducers (shape, size), electrode material depending on the characteristics of the object (different ability to conduct current, different concentration ranges, the abi-

lity of electrodes to adsorb) and test conditions, frequency ranges, temperatures, test signal level ranges).

4. Impedance spectra investigation

4.1. Equivalent low-impedance substitution schemes

Based on computer simulation of the impedance spectra (obtained by experiment for a system with two electrodes made of stainless steel in the form of plates), conducted with the EIS Spectrum Analyzer soft, the values of the substitution circuit elements (Fig. 1, a) were calculated (for example NaCl) of different concentrations ($c = (1\div 9)$ g/l) and at different frequency ranges. The program performs modeling based on the Levenberg–Marquardt algorithm, which is one of the optimization methods and is a modification of Newton's method (Fig. 1). The results of the computer simulation of the electrode-electrolyte system are presented in Table 1.

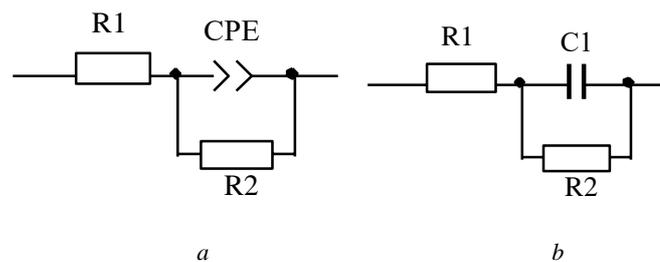


Fig. 1. Electrode-electrolyte system substitution schemes (aqueous NaCl salt solution) for frequencies not exceeding 1 kHz: C1 is the double electric layer capacitance, CPE is the constant phase element, R1 is the electrolyte resistance, R2 is the interphase transition resistance

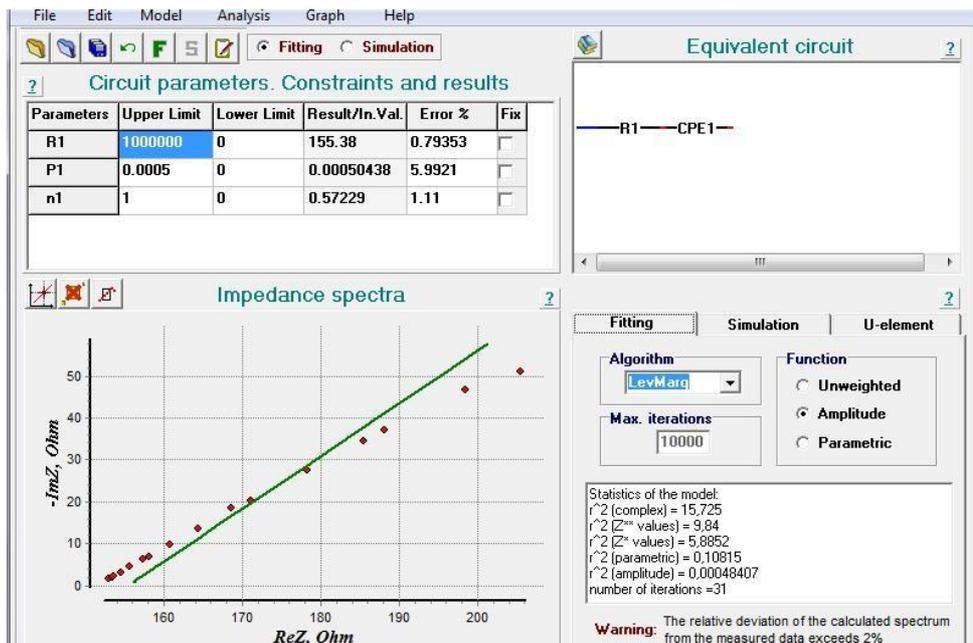


Fig. 2. EIS Spectrum Analyzer interface of salt solution impedance spectrum analysis

Table 1

Reproduction of the values of the substitution scheme elements (Fig. 1, a) within different frequency ranges for different values of the aqueous salt solution concentration

| <i>C</i> , g/l | <i>F</i> , Hz | <i>R</i> ₁ , Ohm | δ_{R1} , % | <i>R</i> ₂ , Ohm | δ_{R2} , % | <i>P</i> | δ_P , % | <i>n</i> | δ_n , % |
|----------------|---------------|-----------------------------|-------------------|-----------------------------|-------------------|------------|----------------|----------|----------------|
| 1 | 50÷100000 | 153.01 | 0.47 | 536.06 | 42 | 0.00050498 | 3.57 | 0.55389 | 0.88 |
| 1 | 50÷1000 | 153.7 | 1.089 | 575.86 | 70 | 0.00050496 | 5.09 | 0.55668 | 1.33 |
| 1 | 1000÷100000 | 7143 | 33.4 | 49188 | >1000 | 0.0000043 | >1000 | 1.01 | >1000 |
| 2 | 50÷100000 | 51.56 | 1.34 | 138.28 | 32.34 | 0.00050494 | 6.84 | 0.6292 | 1.38 |
| 2 | 50÷1000 | 52.66 | 1.16 | 143.91 | 53.52 | 0.00050495 | 9.45 | 0.6365 | 2.07 |
| 2 | 1000÷100000 | 50.31 | 0.35 | 85.21 | 67.56 | 0.00050494 | 3.22 | 0.5859 | 0.55 |
| 3 | 50÷100000 | 30.03 | 2.06 | 93.24 | 30.48 | 0.00050497 | 8.54 | 0.6552 | 1.58 |
| 3 | 50÷1000 | 32.65 | 16.15 | 41.11 | 45.83 | 0.00005376 | 70.27 | 0.9916 | 6.99 |
| 3 | 1000÷100000 | 29.03 | 0.52 | 53.56 | 52.05 | 0.00050497 | 3.88 | 0.6078 | 0.63 |
| 4 | 50÷100000 | 21.88 | 2.6 | 88.19 | 29 | 0.00050494 | 8.93 | 0.65728 | 1.59 |
| 4 | 50÷1000 | 23.28 | 6.21 | 94.19 | 48.5 | 0.00050495 | 11.5 | 0.67074 | 2.29 |
| 4 | 1000÷100000 | 21.4 | 1.59 | 5.83 | >1000 | 0.00050135 | 11.6 | 0.62845 | 1.66 |
| 5 | 50÷100000 | 16.29 | 4.46 | 66.82 | 26.27 | 0.00047882 | 14.01 | 0.67312 | 2.30 |
| 5 | 50÷1000 | 17.98 | 7.82 | 75.35 | 54.14 | 0.00050495 | 12.67 | 0.69000 | 2.44 |
| 5 | 1000÷100000 | 16.31 | 2.19 | 2.79 | >1000 | 0.00047334 | 14.95 | 0.65154 | 2.02 |
| 6 | 50÷100000 | 13.36 | 6.77 | 53.56 | 35.71 | 0.00050493 | 15.09 | 0.66605 | 2.55 |
| 6 | 50÷1000 | 1.60 | 414 | 30.78 | 35.69 | 0.00004022 | 229.3 | 0.78856 | 16.8 |
| 6 | 1000÷100000 | 13.72 | 2.74 | 9.345 | >1000 | 0.00046512 | 17.63 | 0.65988 | 2.32 |
| 7 | 50÷100000 | 10.12 | 11.1 | 49.71 | 27.45 | 0.00050491 | 19.25 | 0.6678 | 2.88 |
| 7 | 50÷1000 | 12.42 | 11.2 | 52.24 | 49.13 | 0.00050495 | 15.39 | 0.70792 | 2.76 |
| 7 | 1000÷100000 | 10.65 | 3.75 | 7.86 | >1000 | 0.00047876 | 20.25 | 0.66123 | 2.61 |
| 8 | 50÷100000 | 9.52 | 5.34 | 48.95 | 32.49 | 0.00050495 | 14.02 | 0.69252 | 2.16 |
| 8 | 50÷1000 | 10.90 | 13.06 | 48.04 | 66.44 | 0.00050499 | 15.65 | 0.71364 | 2.89 |
| 8 | 1000÷100000 | 9.25 | 4.30 | 7.36 | >1000 | 0.00049293 | 21.38 | 0.66301 | 2.72 |
| 9 | 50÷100000 | 8.87 | 5.6 | 48.25 | 34.3 | 0.00050498 | 14.9 | 0.69617 | 2.27 |
| 9 | 50÷1000 | 7.58 | 43.22 | 34.05 | 137.7 | 0.00050493 | 29 | 0.67747 | 5.40 |
| 9 | 1000÷100000 | 8.63 | 4.8 | 5.96 | >1000 | 0.00045809 | 23.8 | 0.67416 | 2.94 |

An electric current passes through the electrode-solution interface. There arises a resistance *R*₂ caused by charge transmission, which characterizes the reaction between the electrode-electrolyte interface. Since the impedance is calculated from current and voltage values, it is logical to apply electrical equivalent schemes; nevertheless, the classical electrical quantities are not enough to describe exactly the variety of real processes and objects. So special electrochemical elements are applied. One of these is the constant phase element (CPE), or the element with a constant angle of loss. The movement of ions in solution occurs due to the diffusion of different concentrations of ions in individual parts of the electrolyte, their convection due to the capture by the flow of moving fluid, the migration of ions under the impact of an electric field, thermal phenomena.

Analysis of the Table 1 showed that at frequencies higher than 1000 Hz, the substitution scheme (Fig. 1, a) is not suitable for reproducing the saline solution properties since the circuit element *R*₂ is the interphase resistance (or diffusion process resistance). The latter is reproduced with an error of ~1000 %.

It should be noted that the simulation of the impedance of the electrolyte solution with the resistance

*R*₁ is valid for highly concentrated solutions within a wide range of frequencies. Only at frequencies exceeding (1÷5) MHz, it is necessary to introduce additional elements that describe the relaxation in the electrolyte. As the concentration of the saline solution increases, the resistance values of the electrolyte *R*₁ fall. The values of the impedance components of the CPE are quite stable. The average value of the exponential index *n* = 0.654, which is included in the formula for calculating the impedance *Z*_{CPE} of this element:

$$Z_{CPE}(j\omega) = P^{-1} (j\omega)^{-n}, \quad (1)$$

and this corresponds to the case of modeling by the CPE of the process of diffusion of electrolyte ions to the interfacial electrode-electrolyte boundary, the transfer of a substance due to the equalization of its concentration (more precisely, chemical potential) in an inhomogeneous system approaching homogeneous. The unit of measurement of the coefficient *P* is equal to the unit of measurement of the Warburg coefficient λ (impedance due to diffusion processes of charge transfer) Ohm·c^{-1/2}. It is believed that there exists a relationship between CPE and the surface roughness of the electrode; so the smoother the electrode surface, the

faster n approaches the unit and becomes exclusively capacitive, the CPE is a measure of the degree of inhomogeneity of the electrode. Therefore, for an ideal geometry of the electrode working surface in the impedance sense, a homogeneous electric field, which is provided by the configuration of the cell, the impedance of its double layer can be represented by capacitance $C1$ (Fig. 1, b; 3, a).

To analyze the circuit (Fig. 3, b) a simulation has been performed (the results are summarized in Table 2). Analysis of Table 1 data shows that at high frequencies (1000÷100000 Hz) the reproduction error of the elements of the substitution scheme (Fig. 3, b) is quite small compared to the substitution scheme (Fig. 1, a). The error of reproduction of the resistance of the studied electrolyte at high frequencies is several times smaller compared to the low-frequency range and is almost invariant to the solution concentration (Fig. 4).

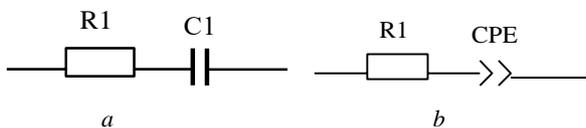


Fig. 3. Substitution scheme of the electrode-electrolyte system: a – for a perfectly polarized electrode, on which no electrochemical reaction occurs; b – in the presence of diffusion phenomena in the electrode region and the flow of Faraday current due to electrode reactions

However, in the low-frequency range of the resistance values reproduction error for the test object

increases rapidly with the electrolyte concentration (Fig. 4).

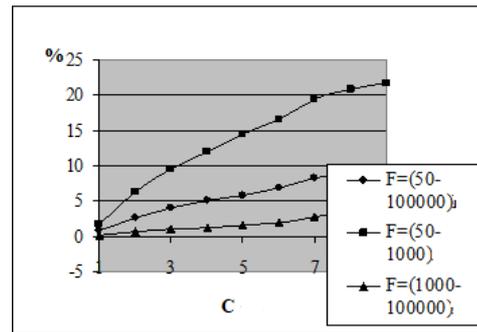


Fig. 4. Dependence of relative errors of resistance values reproduction of electrolyte according to the substitution scheme in Fig. 3 on concentration changes

Therefore, it was proposed to investigate in different frequency ranges the equivalent scheme (Fig. 5), which in comparison with the circuit of Fig. 1, a is supplemented by an element $C1$ simulating the capacitance of the electrode layer.

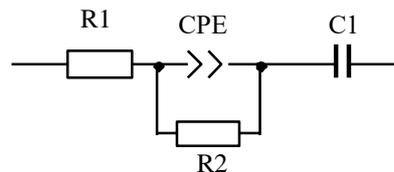


Fig. 5. Substitution scheme of the electrode-electrolyte system, taking into account the electrode capacity $C1$

Table 2

Reproduction of the values of the elements of substitution scheme elements (Fig. 3, b) in different frequency ranges for different values of the aqueous salt solution concentration

| C, g/l | F, Hz | R1, Ohm | $\delta_{R1}, \%$ | P | $\delta_P, \%$ | n | $\delta_n, \%$ |
|--------|-------------|---------|-------------------|------------|----------------|---------|----------------|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 1 | 50÷100000 | 155.38 | 0.79 | 0.00050438 | 5.99 | 0.57229 | 1.11 |
| 1 | 50÷1000 | 158.18 | 1.68 | 0.00050496 | 7.64 | 0.57723 | 1.66 |
| 1 | 1000÷100000 | 151.92 | 0.18 | 0.00049368 | 2.44 | 0.53551 | 0.43 |
| 2 | 50÷100000 | 54.26 | 2.67 | 0.00047582 | 16.5 | 0.67971 | 2.35 |
| 2 | 50÷1000 | 58.29 | 6.31 | 0.00044873 | 19.5 | 0.70323 | 3.21 |
| 2 | 1000÷100000 | 50.82 | 0.60 | 0.00047418 | 6.82 | 0.60586 | 1.02 |
| 3 | 50÷100000 | 32.29 | 3.93 | 0.00050500 | 18.50 | 0.70704 | 2.51 |
| 3 | 50÷1000 | 35.97 | 9.45 | 0.00046501 | 23.97 | 0.73309 | 3.66 |
| 3 | 1000÷100000 | 29.50 | 1.01 | 0.00047961 | 9.09 | 0.62965 | 1.29 |
| 4 | 50÷100000 | 23.81 | 4.98 | 0.00048867 | 22.14 | 0.71123 | 2.82 |
| 4 | 50÷1000 | 27.40 | 11.94 | 0.00047394 | 26.21 | 0.73077 | 3.92 |
| 4 | 1000÷100000 | 21.42 | 1.24 | 0.00048898 | 8.87 | 0.63141 | 1.25 |
| 5 | 50÷100000 | 18.34 | 5.84 | 0.00050497 | 22.2 | 0.73032 | 2.78 |
| 5 | 50÷1000 | 21.84 | 14.5 | 0.00045088 | 29.9 | 0.76204 | 4.20 |
| 5 | 1000÷100000 | 16.29 | 1.61 | 0.00049194 | 10.5 | 0.64697 | 1.43 |
| 6 | 50÷100000 | 15.59 | 6.75 | 0.00050498 | 26.4 | 0.74110 | 3.14 |
| 6 | 50÷1000 | 19.14 | 16.5 | 0.00045494 | 33.3 | 0.77474 | 4.51 |
| 6 | 1000÷100000 | 13.68 | 1.97 | 0.00050330 | 11.86 | 0.65062 | 1.59 |

Continuation of Table 2

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|---|-------------|-------|------|------------|-------|---------|------|
| 7 | 50÷100000 | 12.26 | 8.23 | 0.00050496 | 32.06 | 0.74755 | 3.60 |
| 7 | 50÷1000 | 15.92 | 19.4 | 0.00045885 | 37.17 | 0.78453 | 4.85 |
| 7 | 1000÷100000 | 10.62 | 2.78 | 0.00050470 | 13.99 | 0.65502 | 1.82 |
| 8 | 50÷100000 | 10.75 | 9.02 | 0.00050490 | 34.41 | 0.75516 | 3.77 |
| 8 | 50÷1000 | 14.33 | 20.8 | 0.00045771 | 39.9 | 0.79273 | 5.08 |
| 8 | 1000÷100000 | 9.25 | 3.27 | 0.00049790 | 15.4 | 0.66183 | 1.96 |
| 9 | 50÷100000 | 10.01 | 9.43 | 0.00050491 | 33.9 | 0.75841 | 3.70 |
| 9 | 50÷1000 | 13.56 | 21.6 | 0.00045153 | 39.2 | 0.79840 | 4.97 |
| 9 | 1000÷100000 | 8.59 | 3.51 | 0.00050247 | 15.8 | 0.66328 | 2.01 |

Table 3

Reproduction of the element values of the substitution scheme (Fig. 5) in different frequency ranges for different values of the concentration of the aqueous salt solution

| C g/ l | F, Hz | R1, Ohm | δ_{R1} , % | C1, μ F | δ_{C1} , % | R2, Ohm | δ_{R2} , % | P | δ_P , % | n | δ_n , % |
|--------------|-------------|------------|----------------------|----------------|----------------------|------------|----------------------|------------|-------------------|------|-------------------|
| 1 | 50÷100000 | 151.9 | 0.49 | 144 | 12.9 | 139.6 | 9.2 | 0.00050121 | 3.97 | 0.54 | 0.99 |
| 1 | 50÷1000 | 151.7 | 1.07 | 147 | 21.8 | 139.2 | 14.6 | 0.00048286 | 6.79 | 0.55 | 1.76 |
| 1 | 1000÷100000 | 151.54 | 0.14 | 27 | 12.9 | 39.76 | 11.9 | 0.00045057 | 3.81 | 0.53 | 0.72 |
| 1 | 50÷100000 | 50.47 | 0.95 | 177 | 13.05 | 46.94 | 7.23 | 0.0004654 | 6.76 | 0.61 | 1.37 |
| 2 | 50÷1000 | 53.12 | 3.7 | 145 | 51 | 39.31 | 31.4 | 0.00050177 | 31.7 | 0.61 | 6.63 |
| 2 | 1000÷100000 | 52.11 | 2.66 | 505 | >1000 | 0.00002 | >1000 | 0.00011223 | 63 | 0.78 | 6.12 |
| 3 | 50÷100000 | 29.37 | 1.22 | 216 | 14.2 | 35.34 | 7.99 | 0.00045062 | 7.48 | 0.64 | 1.39 |
| 3 | 50÷1000 | 30.41 | 2.76 | 251 | 21.7 | 39.65 | 12.29 | 0.00004823 | 9.6 | 0.65 | 1.97 |
| 3 | 1000÷100000 | 28.15 | 3.55 | 357 | >1000 | 15.42 | 69.97 | 0.00019113 | 109 | 0.64 | 11.34 |
| 4 | 50÷100000 | 21.27 | 1.37 | 237 | 12.56 | 36.22 | 8.49 | 0.00050491 | 6.06 | 0.63 | 1.15 |
| 4 | 50÷1000 | 21.71 | 3.43 | 238 | 19.74 | 36.43 | 11.32 | 0.00050373 | 9.39 | 0.64 | 1.96 |
| 4 | 1000÷100000 | 20.94 | 0.28 | 53 | 5.5 | 11.19 | 4.35 | 0.00032127 | 2.12 | 0.65 | 0.31 |
| 5 | 50÷100000 | 16.13 | 1.63 | 251 | 12.9 | 29.48 | 8.47 | 0.00050497 | 6.87 | 0.65 | 1.22 |
| 5 | 50÷1000 | 16.33 | 4.16 | 257 | 17.8 | 29.99 | 10.50 | 0.00050103 | 9.61 | 0.65 | 1.89 |
| 5 | 1000÷100000 | 15.70 | 0.48 | 55 | 13.1 | 9.52 | 7.88 | 0.00048743 | 7.02 | 0.61 | 1.11 |
| 6 | 50÷100000 | 13.49 | 1.87 | 269 | 14.1 | 26.58 | 8.68 | 0.00050493 | 7.65 | 0.65 | 1.31 |
| 6 | 50÷1000 | 13.83 | 4.67 | 278 | 18.9 | 27.04 | 10.43 | 0.00049735 | 10.2 | 0.66 | 1.96 |
| 6 | 1000÷100000 | 15.39 | 13.8 | 329 | >1000 | 0.00004 | >1000 | 0.00019376 | >1000 | 0.66 | >1000 |
| 7 | 50÷100000 | 10.40 | 2.38 | 278 | 15.8 | 23.72 | 9.07 | 0.00050491 | 8.84 | 0.65 | 1.45 |
| 7 | 50÷1000 | 11.43 | 4.88 | 301 | 19.55 | 24.49 | 10.95 | 0.00050083 | 9.80 | 0.68 | 1.87 |
| 7 | 1000÷100000 | 11.04 | 7.38 | 504 | >1000 | 6.55 | >1000 | 0.00022155 | 68.76 | 0.76 | 6.58 |
| 8 | 50÷100000 | 8.94 | 2.91 | 273 | 18.3 | 21.38 | 9.08 | 0.00050496 | 10.72 | 0.65 | 1.71 |
| 8 | 50÷1000 | 9.86 | 5.53 | 317 | 18.29 | 22.97 | 10.63 | 0.0005049 | 9.99 | 0.68 | 1.86 |
| 8 | 1000÷100000 | 9.86 | 10.5 | 234 | >1000 | 4.33 | 496 | 0.00022497 | >1000 | 0.65 | >1000 |
| 9 | 50÷100000 | 8.33 | 3.02 | 274 | 17.96 | 20.59 | 9.65 | 0.00050500 | 10.79 | 0.65 | 1.70 |
| 9 | 50÷1000 | 7.40 | 16.8 | 219 | 67.35 | 18.85 | 23.32 | 0.00050499 | 52 | 0.62 | 8.87 |
| 9 | 1000÷100000 | 8.07 | 0.79 | 75.78 | 9.33 | 7.76 | 5.78 | 0.00037555 | 3.39 | 0.65 | 0.48 |

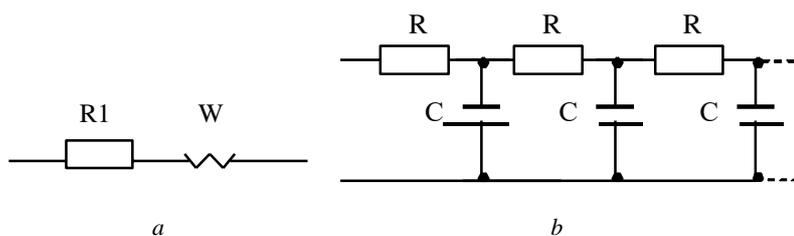


Fig. 6. Warburg impedance: a – the substitution scheme of the electrode-electrolyte system, taking into account the impedance of Warburg; b – and the equivalent Warburg impedance scheme

Analyzing the data in Table 3, it can be concluded that in the low-frequency range it would be possible to apply a model of the type (Fig. 5); in general, there is a manifestation of the CPE as an element characterizing the diffusion of active particles to the electrode-electrolyte interface. So ions move through the electrolyte occurs only due to the diffusion of conduction ions. Near the electrode, the charge transfer processes are determined by diffusion and charge transfer in the diffusion layer, where the diffusion capacity of the Stern

electrode layer is formed. This impedance is called the Warburg diffusion impedance to reflect the impedance of an ideal linear semi-infinite diffusion (Fig. 6, a, b). Notice, the investigated frequencies are not low enough to ensure the penetration of the diffusion sinusoidal wave to the boundary of the real diffusion layer.

Replacement of the CPE with the Warburg element (Fig. 6, a) led to an enhancement in the accuracy of the reproduction of the substitution scheme elements (Table 4).

Table 4

Reproduction of the substitution scheme elements values (Fig. 6) in particular frequency ranges for different values of the concentration of the aqueous salt solution

| C, g/l | F, Hz | R1, Ohm | δ_{R1} , % | AW | Δ_{AW} , % |
|--------|-------------|---------|-------------------|--------|-------------------|
| 1 | 50÷100000 | 152.05 | 0.22 | 932.52 | 1.54 |
| 1 | 50÷1000 | 152.07 | 0.51 | 931.22 | 1.88 |
| 1 | 1000÷100000 | 151.32 | 0.11 | 1063.5 | 2.07 |
| 2 | 50÷100000 | 50.40 | 0.38 | 534.74 | 2.14 |
| 2 | 50÷1000 | 50.56 | 1.11 | 532.81 | 2.46 |
| 2 | 1000÷100000 | 49.80 | 0.18 | 617.79 | 1.82 |
| 3 | 50÷100000 | 29.02 | 0.51 | 435.19 | 2.48 |
| 3 | 50÷1000 | 29.21 | 1.62 | 433.09 | 2.70 |
| 3 | 1000÷100000 | 28.57 | 0.19 | 498.02 | 1.70 |
| 4 | 50÷100000 | 20.93 | 0.65 | 422.83 | 2.77 |
| 4 | 50÷1000 | 21.14 | 2.30 | 420.46 | 2.95 |
| 4 | 1000÷100000 | 20.54 | 0.24 | 478.06 | 1.87 |
| 5 | 50÷100000 | 15.74 | 0.69 | 372.29 | 2.58 |
| 5 | 50÷1000 | 15.89 | 2.49 | 370.43 | 2.81 |
| 5 | 1000÷100000 | 15.46 | 0.27 | 414.64 | 1.95 |
| 6 | 50÷100000 | 13.21 | 0.90 | 345.61 | 3.41 |
| 6 | 50÷1000 | 13.51 | 3.12 | 342.07 | 3.24 |
| 6 | 1000÷100000 | 12.88 | 0.29 | 392.97 | 2.03 |
| 7 | 50÷100000 | 10.21 | 1.33 | 323.85 | 4.31 |
| 7 | 50÷1000 | 10.67 | 4.16 | 317.86 | 3.63 |
| 7 | 1000÷100000 | 9.84 | 0.48 | 378.34 | 2.18 |
| 8 | 50÷100000 | 8.83 | 1.51 | 307.98 | 4.54 |
| 8 | 50÷1000 | 9.31 | 4.52 | 301.4 | 3.69 |
| 8 | 1000÷100000 | 8.48 | 0.58 | 361.51 | 2.35 |
| 9 | 50÷100000 | 8.16 | 1.48 | 302.62 | 4.07 |
| 9 | 50÷1000 | 8.61 | 4.26 | 296.17 | 3.32 |
| 9 | 1000÷100000 | 7.85 | 0.65 | 353.36 | 2.47 |

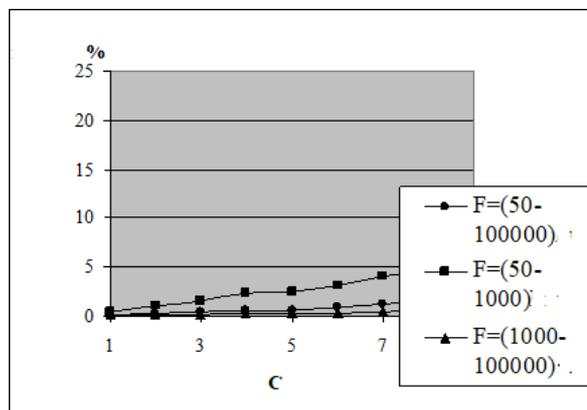


Fig. 7. Dependence of the relative errors of reproduction of the resistance values of the electrolyte according to the substitution scheme in Fig. 6 a on the values of its concentration

Comparison of the dependences of the reproduction errors of the substitution scheme elements containing the CPE (Table 3) and the Warburg element (Table 4) allowed us to conclude that at frequency band 50–1000 Hz the equivalent scheme can be represented by Fig. 6, *a* and the Warburg impedance (Fig. 6, *b*) adequately describes the processes occurring in the test system at higher frequencies (from 1–100 kHz), at which the electrode effects practically disappear.

4.2. Equivalent substitution schemes for high-impedance objects

Biochemical systems based on natural materials, in particular sugar solutions, are of interest for research of high-resistance objects. Based on the data of impedance measurements, their analysis was performed and the corresponding structure of the substitution scheme was obtained (Fig. 8).

Since these are polarized electrodes, the substitution scheme contains a link that describes the presence of the capacitance $C1$ in the electrode Helmholtz layer and the resistance of charge transfer $R1$. The presence of the CRE in the substitution scheme is explained by the inhomogeneity of the electrode surface, which may be caused by the selective adsorption of sugar on the electrodes, or even by the presence of a small amount of gas (air oxygen), which leads to the formation of phase boundaries (fractals). The latter produces the local alteration in the electrochemical parameters of the electrode surface, which is best modeled by CPE. To eliminate this phenomenon, it is recommended to create closed-type electrochemical cells for minimization of contact of the solution with air. Elements of the substitution scheme were reproduced with sufficient accuracy from 0.2 % to 4 % for different concentrations of sugar solutions (Table 5).

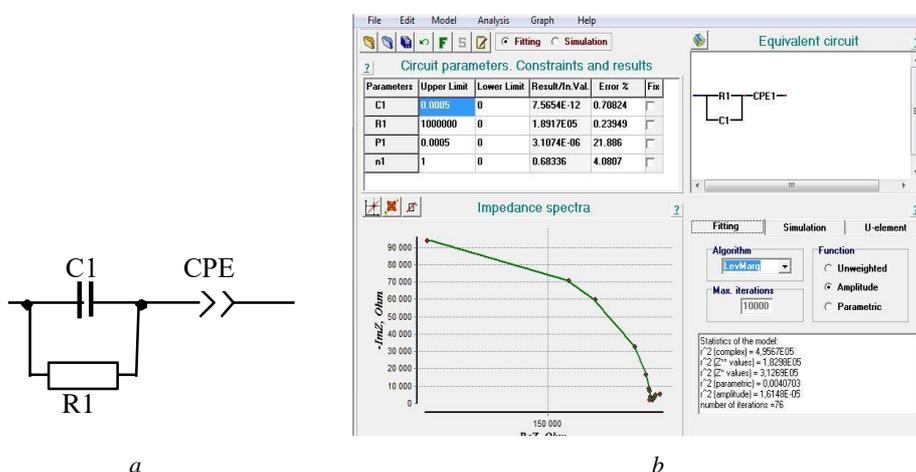


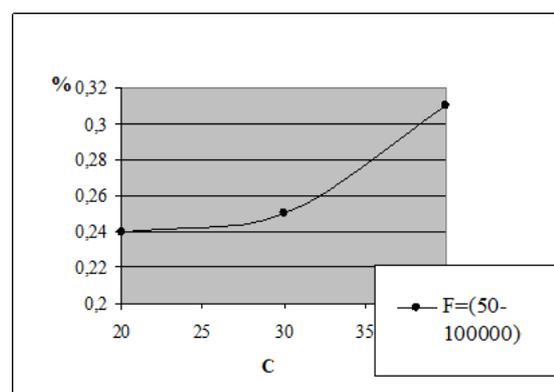
Fig. 8. Modeling of the electrochemical system of aqueous sugar solution: *a* – the substitution scheme of the electrode – non-electrolyte system for aqueous sugar solution); *b* – the impedance spectrum of the sugar solution

Table 5

Reproduction of the substitution scheme elements values (Fig. 8) in particular frequency ranges for different values of the concentration of aqueous sugar solution

| C , g/l | F , Hz | $R1$, Ohm | δ_{R1} , % | $C1$, pF | δ_{C1} , % | P | δ_P , % | n | δ_n , % |
|-----------|-----------|------------|-------------------|-----------|-------------------|-----------|----------------|---------|----------------|
| 20 | 50÷100000 | 189170 | 0.24 | 7.6 | 0.7 | 0.0000031 | 11.9 | 0.68336 | 4.1 |
| 30 | 50÷100000 | 122720 | 0.25 | 7.4 | 0.9 | 0.000010 | 11.1 | 0.49843 | 3.2 |
| 40 | 50÷100000 | 80065 | 1.31 | 7.2 | 1.4 | 0.000004 | 10.7 | 0.67296 | 2.2 |

Fig. 9. Dependence of the relative errors of the resistance values reproduction of the solution according to the substitution scheme in Fig. 8, *a* on the values of its concentration



The error of reproduction of the test object resistance increases with concentration (Fig. 9). This may indicate that the equivalent scheme may also differ for appropriate concentration ranges as in the case of different frequency subranges.

5. Conclusions

The study of impedance spectra of non-electrical nature objects has been fulfilled. Equivalent substitution schemes have been developed for objects independent of their resistance.

In particular, for low-resistance objects – salt solutions, circuits containing the capacity of the double electric layer and circuits with a constant phase element were synthesized. Data analysis showed that at frequencies higher than 1000 Hz, the substitution scheme, the capacity of the double electric layer, is not suitable for reproducing the properties of saline solution because the resistance between the phase transition (or the resistance of the diffusion process) is reproduced with errors exceeding 1000 %. It is proved that the resistance simulation of the impedance of the electrolyte solution is valid for highly concentrated solutions in a wide range of frequencies. Only at frequencies exceeding (1÷5) MHz, it is necessary to introduce additional elements considering the relaxation in the electrolyte.

There were studied the diffusion phenomena in the electrode. Comparison of the dependences of reproduction errors of substitution scheme elements containing a constant phase element and a Warburg element is available at frequencies range 50–1000 Hz.

The equivalent circuit of a low-impedance object can be represented by a constant phase element and the Warburg impedance that adequately describes the system at high frequencies (1–100 kHz). Furthermore, the electrode effects almost fall.

For high-resistance objects, it is recommended to create closed-type electrochemical cells that minimize the contact area “solution – air”.

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7. Conflict of interest

The authors state that there are no financial or other potential conflicts regarding this work.

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